Name $\qquad$
$\qquad$

## Reteaching with Practice

For use with pages 551-557

GOAL Find the side lengths of special right triangles

## Vocabulary

Right triangles whose angle measures are $45^{\circ}-45^{\circ}-90^{\circ}$ or $30^{\circ}-60^{\circ}-90^{\circ}$ are called special right triangles.

Theorem 9.8 The $\mathbf{4 5}^{\circ}-\mathbf{4 5}^{\circ}$ - $90^{\circ}$ Triangle Theorem
In a $45^{\circ}-45^{\circ}-90^{\circ}$ triangle, the hypotenuse is $\sqrt{2}$ times as long as each leg.
Theorem 9.9 The $30^{\circ}-60^{\circ}-90^{\circ}$ Triangle Theorem
In a $30^{\circ}-60^{\circ}-90^{\circ}$ triangle, the hypotenuse is twice as long as the shorter leg, and the longer leg is $\sqrt{3}$ times as long as the shorter leg.

## EXAMPLE 1 Finding Side Lengths in a $45^{\circ}-45^{\circ}-90^{\circ}$ Triangle

Find the value of $x$.


## Solution

By the Triangle Sum Theorem, the measure of the third angle is $45^{\circ}$. The triangle is a $45^{\circ}-45^{\circ}-90^{\circ}$ right triangle, so the length $x$ of the hypotenuse is $\sqrt{2}$ times the length of a leg.

$$
\begin{aligned}
\text { Hypotenuse } & =\sqrt{2} \cdot \text { leg } & & 45^{\circ}-45^{\circ}-90^{\circ} \text { Triangle Theorem } \\
x & =\sqrt{2} \cdot 7 & & \text { Substitute. } \\
x & =7 \sqrt{2} & & \text { Simplify. }
\end{aligned}
$$

## Exercises for Example 1

Find the value of each variable.
1.

2.

3.

$\qquad$

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## EXAMPLE 2 Finding Side Lengths in a $30^{\circ}-60^{\circ}-90^{\circ}$ Triangle

Find the value of $x$.


## Solution

Because the triangle is a $30^{\circ}-60^{\circ}-90^{\circ}$ triangle, the longer leg is $\sqrt{3}$ times the length $x$ of the shorter leg.

Longer leg $=\sqrt{3} \cdot$ shorter leg

$$
30^{\circ}-60^{\circ}-90^{\circ} \text { Triangle Theorem }
$$

$$
\begin{aligned}
22 & =\sqrt{3} \cdot x \\
\frac{22}{\sqrt{3}} & =x \\
\frac{\overline{3}}{3} \cdot \frac{22}{\sqrt{3}} & =x \\
\frac{22 \sqrt{3}}{3} & =x
\end{aligned}
$$

Substitute.

Divide each side by $\sqrt{3}$.

$$
\frac{\sqrt{3}}{\sqrt{3}} \cdot \frac{22}{\sqrt{3}}=x \quad \text { Multiply numerator and denominator by } \sqrt{3}
$$

Simplify.

## Exercises for Example 2

Find the value of each variable.
4.

5.

6.


