LESSON 4.1

Challenge: Skills and Applications

For use with pages 194–201

- **1.** a. Find $m \angle 1 + m \angle 2 + m \angle 3 + m \angle 4 + m \angle 5 + m \angle 6$.
 - **b.** Find the sum of the measures of the exterior angles of the triangle.
 - **c.** Prove your result in part (b).

NAME



- **2.** Use the diagram to find the values of *x* and *y*.
- **3.** A *polyhedron* is a solid figure whose exterior surface is made up of polygons; each of these polygons is called a *face* of the polyhedron. The *defect* of a polyhedron is $(360n S)^\circ$, where *n* is the number of vertices and *S* is the sum of all of the angle measures in all of the faces. In this exercise, we will consider only those polyhedra whose faces are triangles.



- a. Find the defects of the two polyhedra shown.
- **b.** A *regular icosahedron* is a polyhedron with 20 faces that are equiangular triangles and with 12 vertices. What is the defect of a regular icosahedron?
- **c.** Make a conjecture about the defect of a polyhedron whose faces are all equiangular triangles.
- **d.** Do you think your conjecture is true for any polyhedron with triangular faces, even if the triangles are not equiangular? Explain.
- **4. a.** Find $m \angle RQT$ in terms of x and/or y.
 - **b.** What assumption would you need to make in order to find $m \angle QST$ in terms of x and/or y? Under this assumption, what is $m \angle QST$?



- **5. a.** Suppose the ratio of the angle measures of a triangle is 2:3:4. Find the measure of each angle.
 - **b.** Suppose the ratio of the angle measures of a triangle is *a*:*b*:*c*, where *a*, *b*, and *c* are positive numbers. Find the measure of each angle in terms of *a*, *b*, and *c*.

22

Lesson 4.1

Date