

Challenge: Skills and Applications

For use with pages 165–171

In Exercises 1–6, write an equation of the line that passes through point P and has the given slope. Use slope-intercept form.

1. $(12, d)$; $m = \frac{3}{4}$
2. $(c, -4)$; $m = 2$
3. $(-3, g)$; $m = 4r$
4. $(r, 7)$; $m = \frac{t}{5}$
5. $(2s, 3t)$; $m = \frac{p}{q}$
6. $\left(\frac{u}{5}, \frac{v}{3}\right)$; $m = 2$

In Exercises 7–12, write an equation of the line that passes through point P and is parallel to the line with the given equation. Use slope-intercept form.

7. $(0, p)$; $y = 3x - 4$
8. (c, d) ; $y = 4x - 5$
9. $(3, -5)$; $6x - y = 21$
10. $(-10, 4)$; $2x + y = W$
11. $(1, 4)$; $Ax + By = C$
12. $(b, 4d)$; $x - ty = s$
13. Let $A(0, u)$ and $C(0, v)$ be two points on the y -axis. Let $B(w, 0)$ and $D(x, 0)$ be two points on the x -axis. If $\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$, express x in terms of u , v , and w .

In Exercises 14–16, suppose the points $O(0, 0)$, $D(q, r)$, and $E(s, t)$ are three noncollinear points. Find the coordinates of the given point.

14. F , given that $\overleftrightarrow{OD} \parallel \overleftrightarrow{EF}$ and $\overleftrightarrow{DF} \parallel \overleftrightarrow{OE}$
15. G , given that $\overleftrightarrow{ED} \parallel \overleftrightarrow{GO}$ and $\overleftrightarrow{EG} \parallel \overleftrightarrow{DO}$
16. H , given that $\overleftrightarrow{DH} \parallel \overleftrightarrow{EO}$ and $\overleftrightarrow{OH} \parallel \overleftrightarrow{ED}$
17. Consider the two linear equations $Ax + By = C$ and $Dx + Ey = F$.
 - a. If the lines described by these equations are parallel, what condition must be satisfied by A , B , D , and E ?
 - b. If the condition you wrote is satisfied, are there any values of C and F for which the equations do *not* describe two parallel lines? Explain.