

# Challenge: Skills and Applications

For use with pages 136–141

1. Write a two-column proof.

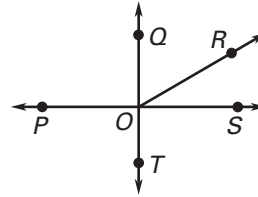
**Given:**

$\angle POT$  and  $\angle TOS$  are a linear pair.

$\angle POT \cong \angle TOS$

**Prove:**

$\angle QOR$  and  $\angle ROS$  are complementary.



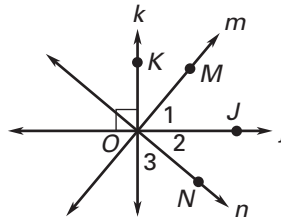
2. Write a paragraph proof.

**Given:**

$j \perp k$ ;  $\angle 1 \cong \angle 3$

**Prove:**

$m \perp n$



3. Write a flow proof.

**Given:**

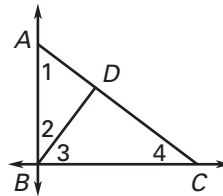
$\angle 1$  and  $\angle 2$  are complementary;

$\angle 1$  and  $\angle 4$  are complementary;

$\angle 4$  and  $\angle 3$  are complementary.

**Prove:**

$\overleftrightarrow{AB} \perp \overleftrightarrow{BC}$



**In Exercises 4–9, sketch the situation, if possible, or explain why it is not possible.**

4.  $\angle QOP$  and  $\angle QOR$  are complementary, but  $\angle POR$  is not a right angle.

5.  $\angle WXY$  and  $\angle WXZ$  are supplementary, and  $\angle YXZ$  is a right angle.

6.  $\overrightarrow{EG}$  bisects  $\angle DEF$ , and  $\overrightarrow{EG} \perp \overrightarrow{DE}$ .

7.  $\angle DEG$  and  $\angle GEF$  are complementary,  $\overrightarrow{EG} \perp \overrightarrow{DF}$ , and  $\overrightarrow{EG}$  bisects  $\angle DEF$ .

8. There are three lines,  $p$ ,  $q$ , and  $r$ , such that  $p \perp q$ ,  $q \perp r$ , and  $p \perp r$ .

9.  $A$ ,  $B$ , and  $C$  are distinct points such that  $A$  and  $B$  are on line  $j$ ;  $\overleftrightarrow{AC} \perp j$ ;  $\overleftrightarrow{BC} \perp j$ .