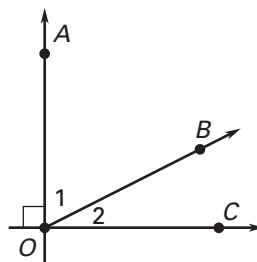


Challenge: Skills and Applications

For use with pages 109–116

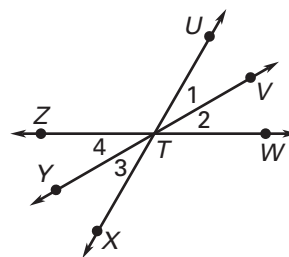
1. a. Use the diagram shown to write a two-column proof of the following theorem: If the nonshared sides of two adjacent acute angles are perpendicular, then the angles are complementary.
 b. Explain why the word *acute* is necessary in the statement of the theorem.
 c. Explain how your proof used the fact that the angles are acute.



2. Write a two-column proof.

Given: \overrightarrow{TV} bisects $\angle UTW$

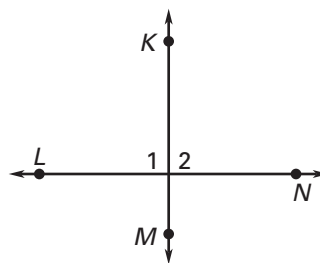
Prove: \overrightarrow{TY} bisects $\angle XTZ$



3. Write a paragraph proof to show that if two lines form congruent adjacent angles, then the lines are perpendicular.

Given: $\angle 1 \cong \angle 2$

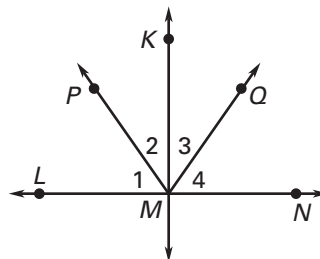
Prove: $\overleftrightarrow{KM} \perp \overleftrightarrow{LN}$



4. Write a paragraph proof. You may use the result of Exercise 3.

Given: \overrightarrow{MK} bisects $\angle PMQ$; $\angle 1 \cong \angle 4$

Prove: $\angle 1$ and $\angle 2$ are complementary.



5. In the diagram, \overrightarrow{OB} bisects $\angle AOC$, and \overrightarrow{OD} bisects $\angle COE$.

- a. Make a conjecture about the relationship between \overrightarrow{OB} and \overrightarrow{OD} .
- b. Write a two-column proof that your conjecture is correct.

