Reteaching with Practice

For use with pages 699-705

GOAL

Find a geometric probability

Vocabulary

A **probability** is a number from 0 to 1 that represents the chance that an event will occur.

Geometric probability is a probability that involves a geometric measure such as length or area.

Probability and Length Let \overline{AB} be a segment that contains the segment \overline{CD} . If a point K on \overline{AB} is chosen at random, then the probability that it is on \overline{CD} is as follows:

$$P(\text{Point } K \text{ is on } \overline{CD}) = \frac{CD}{AB} = \frac{\text{Length of } \overline{CD}}{\text{Length of } \overline{AB}}$$

Probability and Area Let J be a region that contains region M. If a point *K* in *J* is chosen at random, then the probability that it is in region M is as follows:

$$P(\text{Point } K \text{ is in region } M) = \frac{\text{Area of } M}{\text{Area of } J}$$

EXAMPLE 1

Finding a Geometric Probability

Find the probability that a point chosen at random on \overline{AB} is on \overline{CD} .



SOLUTION

$$P(\text{Point is on } \overline{CD}) = \frac{\text{Length of } \overline{CD}}{\text{Length of } \overline{AB}} = \frac{8}{12} = \frac{2}{3}$$

The probability can be written as $\frac{2}{3}$, or approximately 0.667, or 66.7%.

Exercises for Example 1

In Exercises 1-4, find the probability that a point A, selected randomly on AB, is on the given segment.

A
 C
 E
 D
 F
 B
 1.

$$\overline{CD}$$
 2.
 \overline{EF}
 ϕ
 +
 ϕ
 +
 ϕ
 +
 ϕ
 -
 ϕ

1.
$$\overline{CD}$$

3.
$$\overline{CF}$$

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EXAMPLE 2

Using Areas to Find a Geometric Probability

Find the probability that a point chosen at random in parallelogram *ABCD* lies in the shaded region.

A 5 5 C

SOLUTION

Find the ratio of the area of the shaded square to the area of the parallelogram.

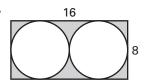
$$P(\text{point is in shaded region}) = \frac{\text{Area of shaded region}}{\text{Area of parallelogram}}$$
$$= \frac{s^2}{bh} = \frac{5^2}{8(5)} = \frac{25}{40} = \frac{5}{8} = 0.625$$

The probability that a point chosen at random in parallelogram *ABCD* lies in the square is 0.625.

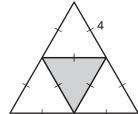
Exercises for Example 2

Find the probability that a point chosen at random in the figure lies in the shaded region.

5.



6.



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