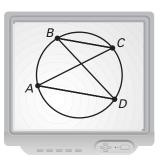
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Use geometry software to construct and investigate a "butterfly" inside a circle.

1. Construct a circle and any four points on the circle. Label the points *A*, *B*, *C*, and *D*, clockwise around the circle. Draw segments *AC*, *BD*, *AD*, and *BC*. The figure that results is called a *butterfly*.

Drag a point of your butterfly along the circle, without crossing other points, to change its shape. Continue to drag points until you have a butterfly whose shape you like. On paper, sketch and label your butterfly.



- **2.** Using your butterfly, measure $\angle ADB$ and $\angle BCA$. Drag points and observe how the angle measures change. What do you notice? What relationship does each angle have with arc *AB*?
- **3.** Predict the relationship between $m \angle DAC$ and $m \angle CBD$ in your butterfly. Measure the angles to check your prediction. With which arc do these angles have a common relationship?
- 4. Construct a new butterfly with center point *M*, the midpoint of a chord YZ as follows: Start with a large circle and construct any chord YZ and its midpoint *M*. Draw any two chords AC and BD that contain *M*. Draw AD and BC, and you have a butterfly. Construct *P*, the intersection of AD and YZ. Construct *Q*, the intersection of BC and YZ. Make and test a conjecture about MP and MQ.



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Lesson 10.3