# ► ACTIVITY 8.1

# **Developing Concepts**

#### SETUP

Work in a small group.

### MATERIALS

- paper
- pencil

# **Investigating Powers**

• **QUESTION** How can you use addition to multiply exponential expressions? How can you use multiplication to raise an exponential expression to a power?

## **EXPLORING THE CONCEPT: PRODUCT OF POWERS**

1 Copy and complete the table. To simplify an expression, expand the product. Then count the factors.

Product of powers	Expanded product	Number of factors	Product as a power
$7^3 \cdot 7^2$	$(7 \cdot 7 \cdot 7) \cdot (7 \cdot 7)$	5	7 <sup>5</sup>
$2^4 \cdot 2^4$	$(2 \cdot 2 \cdot 2 \cdot 2) \cdot (2 \cdot 2 \cdot 2 \cdot 2)$	8	?
$x^4 \cdot x^5$	$(x \cdot x \cdot x \cdot x) \cdot (x \cdot x \cdot x \cdot x \cdot x)$	?	?

2 Add a column to your table that shows the sum of the exponents that are in the first column. What pattern do you notice?

### **EXPLORING THE CONCEPT: POWER OF A POWER**

3 Copy and complete the table. To simplify an expression, expand the product. Then count the factors.

Power of a power	Expanded product	Expanded product	Number of factors	Product as a power
$(5^2)^3$	$(5^2) \cdot (5^2) \cdot (5^2)$	$(5 \cdot 5) \cdot (5 \cdot 5) \cdot (5 \cdot 5)$	6	5 <sup>6</sup>
$[(-3)^2]^2$	$\left[(-3)^2\right] \cdot \left[(-3)^2\right]$	?	?	?
$(b^2)^4$	?	?	?	?

4 Add a column to your table that shows the product of the exponents that are in the first column. What pattern do you notice?

## **DRAWING CONCLUSIONS**

### Expand the product. Then write your answer as a power.

<b>1.</b> $6^3 \cdot 6^2$	<b>2.</b> $(-2) \cdot (-2)^4$	<b>3.</b> $p^4 \cdot p^6$	<b>4.</b> $x^{12} \cdot x^7$
<b>5.</b> (4 <sup>2</sup> ) <sup>6</sup>	<b>6.</b> $[(-5)^2]^4$	<b>7.</b> $(d^5)^5$	<b>8.</b> $[(-n)^3]^8$

9. What operation do you use to simplify a product of powers? Give examples.

- **10**. What operation do you use to simplify a power of a power? Give examples.
- **11. CRITICAL THINKING** Does  $x^3 \cdot y^5 = xy^8$ ? Explain your answer.